

- **Pairs of Lines**
- **Angles**

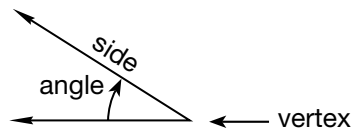
Pairs of Lines

- When lines cross, they **intersect**.
- Lines that go in the same directions and do not intersect are called **parallel lines**.
- Lines that intersect to form square corners are **perpendicular**.
- Intersecting lines that do not form square corners are **oblique**.

Types of Lines			
<p>Parallel Lines</p> <p>Horizontal Vertical Oblique</p>	<p>Parallel Segments</p> <p>Horizontal Vertical Oblique</p>	<p>Intersecting Perpendicular</p> <p>Lines Segments</p>	<p>Intersecting Oblique</p> <p>Lines Segments</p>

Angles

- **Angles** form when lines, line segments, or rays intersect.
- A **vertex** is where 2 sides of an angle meet.



- Angles can be **right**, **acute**, **obtuse**, or **straight**.

<p>Right angle</p> <p>The square corner fits the corner of your paper.</p>	<p>Acute angle</p> <p>Less than a right angle (a cute little angle)</p>	<p>Obtuse angle</p> <p>More than a right angle</p>	<p>Straight angle</p> <p>Makes a straight line, line segment, or ray</p>
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Practice:

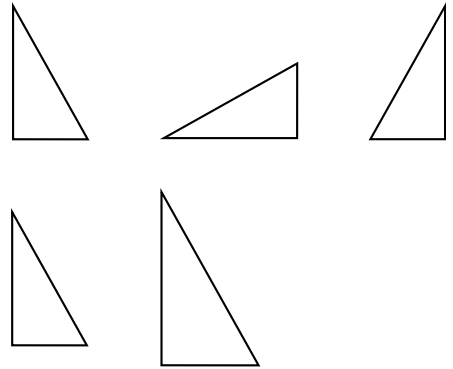
1. Draw two vertical lines.
2. Draw two intersecting oblique line segments.
3. Draw two horizontal line segments.
4. Draw two perpendicular lines.

Draw an example of each angle.

5. right angle
6. obtuse angle
7. acute angle

• **Polygons**

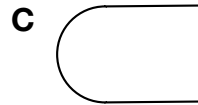
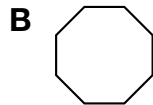
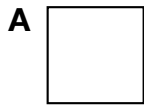
- **Polygons** are closed, flat shapes formed from straight line segments.
- **Congruent** figures have the same shape and size. Their angles and sides match.
- **Similar** figures have the same shape and matching angles but do not have to be the same size.



Practice:

1. Draw a triangle with an obtuse angle.

2. Which shape is not a polygon?



3. Draw two similar, but not congruent rectangles.

4. Can a triangle have more than one right angle? _____

• Rounding Numbers and Estimating

- To make arithmetic easier, we can **round** a number. We “round up” or “round down” to the number that is closest in value to the given number.
- To round a number to the nearest ten, we look at the ones place. If the ones place is less than 5, we round down. If the tens place is equal to or greater than 5, we round up.

Example: Round these numbers to the nearest ten:

$\underline{1}2$ 2 is less than 5, so we round down to 10.

$1\underline{7}$ 7 is greater than 5, so we round up to 20.

- Rounding numbers can help us **estimate** the answer to a problem. Estimated answers are close to, but not equal to, the exact answer.

Example: Estimate 12×17 .

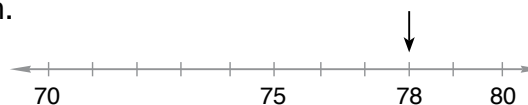
Think $10 \times 20 = 200$. We can estimate that 12×17 is about 200.

- One way to see which number to round a given number to is by using a number line.

Example: Round 78 to the nearest ten.

78 is closer to 80 than 70.

78 rounds up to 80.



Practice:

Round each number to the nearest ten.

1. 54 _____

2. 67 _____

3. 12 _____

4. 85 _____

5. 23 _____

6. 71 _____

Estimate each calculation by rounding two-digit factors to the nearest ten before multiplying.

7. $23 \times 9 =$ _____

8. $4 \times 51 =$ _____

9. $7 \times 67 =$ _____

10. $96 \times 4 =$ _____

• Division with Zeros in the Quotient

- Use the division algorithm (divide, multiply, subtract, “bring down”).
- Place a digit above each digit.
- Use zero as a placeholder when the next digit in the dividend cannot be divided.
- Any number “left over” becomes the remainder.

Examples:

$\begin{array}{r} 106 \text{ R}3 \\ 7 \overline{)745} \\ \underline{7} \\ 04 \\ \underline{0} \\ 45 \\ \underline{42} \\ 3 \end{array}$	$\begin{array}{r} 033 \text{ R}3 \\ 7 \overline{)234} \\ \underline{0} \\ 23 \\ \underline{21} \\ 24 \\ \underline{21} \\ 3 \end{array}$
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Practice:

Divide. Remember to write the dollar sign in money problems.

1. $2 \overline{)19} \text{ R}$

2. $5 \overline{)328} \text{ R}$

3. $3 \overline{)217} \text{ R}$

4. $7 \overline{)609}$

5. $5 \overline{)\$4.25}$

6. $6 \overline{)\$3.72}$

7. $8 \overline{)7100} \text{ R}$

8. $4 \overline{)3210} \text{ R}$

9. $3 \overline{)625} \text{ R}$

10. $2 \overline{)\$8.94}$

11. $9 \overline{)8605} \text{ R}$

12. $7 \overline{)2850} \text{ R}$

• Word Problems About Comparing, and Elapsed Time

- Place the greater number on top.

$$\begin{array}{r} \text{Larger} \\ - \text{Smaller} \\ \hline \text{Difference} \end{array} \qquad \begin{array}{r} \text{Later} \\ - \text{Earlier} \\ \hline \text{Difference} \end{array}$$

- Watch for these keywords in elapsed-time problems.

difference	younger
larger	older
smaller	more
	less

Practice:

Write an equation and solve the problem. Remember to write the units.

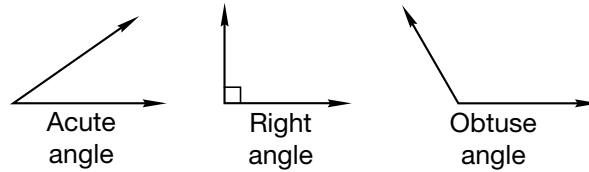
- A kickball team has 6 players. They need 18 players. How many more players does the team need?

- The Empire State Building is 1250 feet tall. If the Sears Tower is 1450 feet tall, how many feet less is the Empire State Building?

- Halley's comet appeared in the sky in 1985. The comet will be visible again in 2061. How many years are there between the times the comet is visible?

• **Classifying Triangles**

- Three types of angles are **acute** angles, **right** angles, and **obtuse** angles.

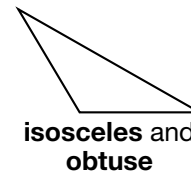
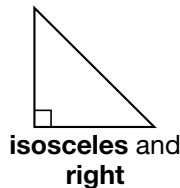
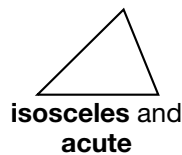


- Triangles can be classified by their **angles**, their **sides**, or both.

Classifying Triangles

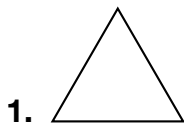
By Sides			By Angles		
Type	Characteristic	Example	Type	Characteristic	Example
Equilateral triangle	Three sides of equal length		Acute triangle	All acute angles	
Isosceles triangle	At least two sides of equal length		Right triangle	One right angle	
Scalene triangle	Three sides of unequal length		Obtuse triangle	One obtuse angle	

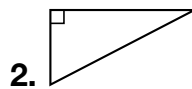
Examples:

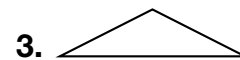


Practice:

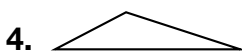
Classify each triangle by its sides.

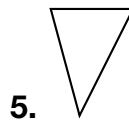


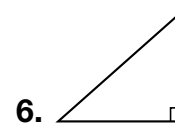




Classify each triangle by its angles.

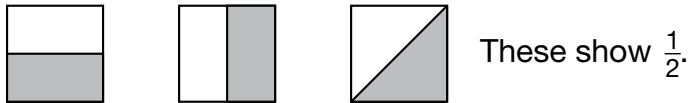




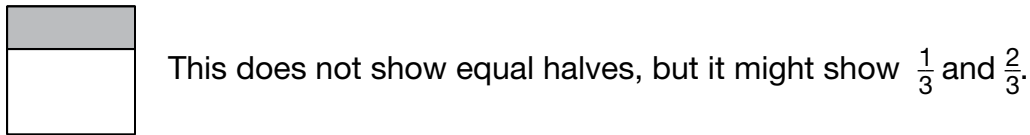


• Drawing Pictures of Fractions

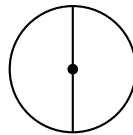
- There are many ways to divide figures into equal fractional parts.



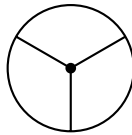
- Remember, not all fractional parts are equal parts.



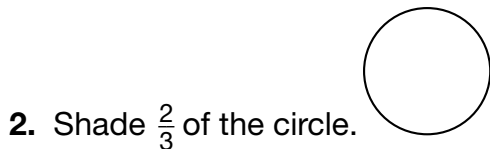
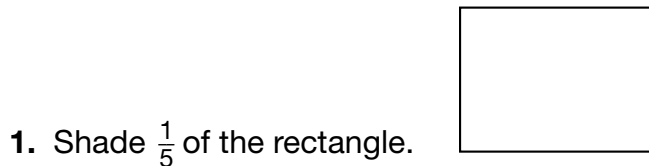
- To divide a circle in half:
 1. Put a point in the center.
 2. Draw a line segment through the center.



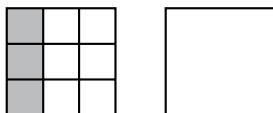
- To divide a circle in thirds:
 1. Put a point in the center.
 2. Draw a "Y" from the center.



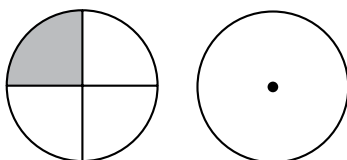
Practice:



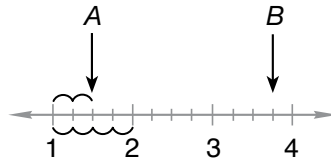
3. The shaded portion of the first square represents the fraction $\frac{3}{9}$.
Use the second square to show another way to shade $\frac{3}{9}$.



4. The shaded portion of the first circle represents the fraction $\frac{1}{4}$.
Use the second circle to show a way to shade $\frac{3}{4}$.



• Fractions and Mixed Numbers on a Number Line

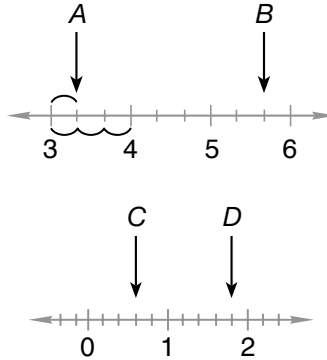


- To identify a fraction or mixed number on a number line:
 1. Count the parts between the whole numbers. (4 parts, so fourths)
 2. Name the arrow as a fraction. (A: $\frac{2}{4}$, B: $\frac{3}{4}$)
 3. Don't forget the whole number. (A: $1\frac{2}{4}$, B: $3\frac{3}{4}$)

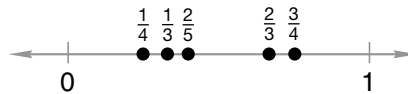
Practice:

Name the fraction or mixed number marked by each arrow on these number lines.

1. A = _____
2. B = _____
3. C = _____
4. D = _____



Three fractions are graphed on the number line below. Refer to the number line to compare the fractions in problems 5–7.

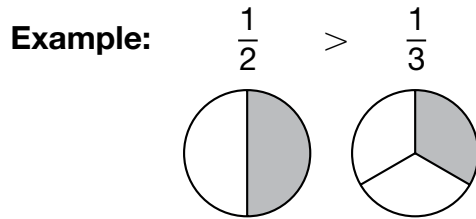


5. $\frac{1}{4} \bigcirc \frac{1}{3}$
6. $\frac{2}{5} \bigcirc \frac{2}{5}$
7. $\frac{1}{2} \bigcirc \frac{2}{3}$
8. Place the following numbers on the number line below. $1\frac{1}{2}$, $1\frac{3}{4}$, $2\frac{1}{4}$



• Comparing Fractions by Drawing Pictures

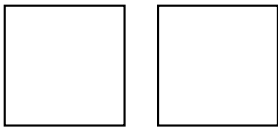
- One way to compare fractions is to draw and shade congruent polygons to represent the fractions. Then we see which polygon is more shaded.



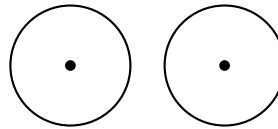
Practice:

Compare each pair of fractions. Draw pictures to illustrate the fractions.

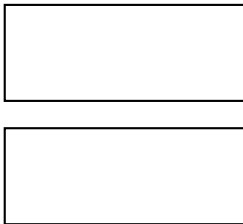
1. $\frac{1}{2} \bigcirc \frac{2}{4}$



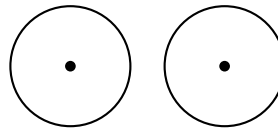
2. $\frac{1}{3} \bigcirc \frac{1}{4}$



3. $\frac{3}{5} \bigcirc \frac{3}{4}$



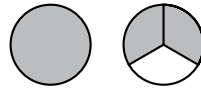
4. $\frac{3}{4} \bigcirc \frac{7}{8}$



• **Writing Quotients with Mixed Numbers**

- To draw pictures that show mixed numbers:
 1. Divide the circles into the parts shown in the **denominator**.
 2. Shade the **whole number** and the parts shown in the **numerator**.

Example:



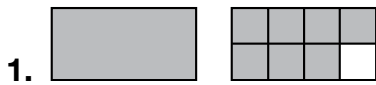
Whole number and a fraction
 $1\frac{2}{3}$

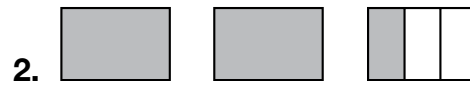
- Some division problems will need the remainder shown as a fraction.
- Write the remainder over the divisor.

Example: $2\overline{)9} \begin{matrix} 4 & R1 \\ \hline 2 & 9 \end{matrix} \rightarrow 4\frac{1}{2}$ ← remainder
← divisor

Practice:

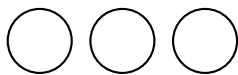
Write a mixed number to name the number illustrated.





Shade the circles to represent each mixed number.

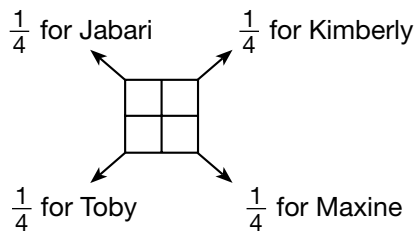
3. two and three fourths



4. three and one third



5. Kimberly, Maxine, Toby, and Jabari will share five sandwiches. How many sandwiches are there for each person?



Show the remainder as a fraction.

$4\overline{)5}$ _____