

## • Multiplying by Two-Digit Numbers

- Use a four-step process to multiply by two-digit numbers.

**Example:** 
$$\begin{array}{r} 25 \\ \times 11 \\ \hline \end{array}$$

- Multiply the ones digits (ignore the tens digit):

$$\begin{array}{r} 25 \\ \times 11 \\ \hline 5 \end{array}$$

- Multiply the tens digit in the top number by the ones digit in the bottom number. Add any number you carried from step 1.

$$\begin{array}{r} 25 \\ \times 11 \\ \hline 25 \end{array}$$

- Indent the next line using zero as a placeholder. Then multiply by the tens digit in the bottom number.

$$\begin{array}{r} 25 \\ \times 11 \\ \hline 25 \\ + 250 \\ \hline \end{array}$$

- Add the two rows.

$$\begin{array}{r} 25 \\ \times 11 \\ \hline 25 \\ + 250 \\ \hline 275 \end{array}$$

- Remember to write the dollar sign and decimal point in money problems.

### **Practice:**

Multiply. Remember to write the dollar sign in money problems.

1. 
$$\begin{array}{r} 52 \\ \times 14 \\ \hline + \phantom{00} \\ \hline \end{array}$$

2. 
$$\begin{array}{r} \$0.85 \\ \times \phantom{00}22 \\ \hline + \phantom{0000} \\ \hline \end{array}$$

3. 
$$\begin{array}{r} 49 \\ \times 67 \\ \hline + \phantom{00} \\ \hline \end{array}$$

4. 
$$\begin{array}{r} 36 \\ \times 24 \\ \hline \end{array}$$

5. 
$$\begin{array}{r} 25 \\ \times 17 \\ \hline \end{array}$$

6. 
$$\begin{array}{r} \$0.72 \\ \times \phantom{00}12 \\ \hline \end{array}$$

• **Naming Numbers through Hundred Billions**

- When we name large numbers we use commas to separate billions, millions, thousands, and ones (units). We do not say “and” when naming whole numbers.

**Example:**

134,652,700,000 → 1 3 4 , 6 5 2 , 7 0 0 , 0 0 0

billions	millions	thousands	units
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one hundred thirty-four billion,  
six hundred fifty-two million,  
seven hundred thousand

- Use the place-value chart below to help name the numbers.

Billions	Millions	Thousands	Units (ones)
hundred billions   ten billions   billions , billions comma	hundred millions   ten millions   millions , millions comma	hundred thousands   ten thousands   thousands , thousands comma	hundreds   tens   ones . decimal point

**Practice:**

Name each number using words.

1. 128,056 \_\_\_\_\_

2. 30,763,000 \_\_\_\_\_

Use digits to write each number in problems 3–4.

3. seven billion, two hundred fifty million \_\_\_\_\_

4. six hundred eight thousand, nine hundred forty-five \_\_\_\_\_

5. In 789,432,177,000 which digit is in the ten billions place? \_\_\_\_\_

6. In which of the following numbers does the 6 have a value of sixty thousand?

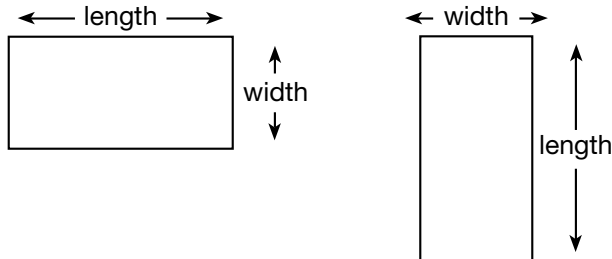
- A** 23,698
**B** 216,783
**C** 468,907
**D** 648,125

7. Write the value of the 3 in 987,654,321. \_\_\_\_\_

• **Perimeter**  
 • **Measures of a Circle**

**Perimeter**

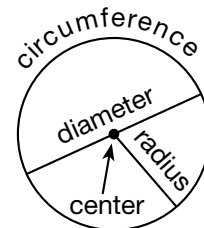
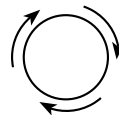
- **Length** is the longer side.
- **Width** is the shorter side.



- **Perimeter** is the distance around a figure.

**Measures of a Circle**

- **Circumference** is the perimeter of a circle.
- The **diameter** of a circle is the distance across the whole circle through its center.



diameter = 2 × radius ( $d = 2r$ )



- The radius of a circle is the distance from its center to its “edge.”

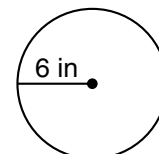
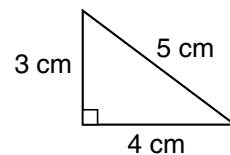
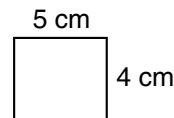
radius =  $\frac{1}{2}$  of diameter ( $r = \frac{1}{2}d$ )



**Practice:**

Remember to write the units.

1. What is the length of the rectangle? \_\_\_\_\_
2. What is the width of the rectangle? \_\_\_\_\_
3. What is the perimeter of the rectangle? \_\_\_\_\_
4. What is the perimeter of the right triangle? \_\_\_\_\_
5. What is the diameter of the circle? \_\_\_\_\_
6. What is the perimeter of a circle called? \_\_\_\_\_



- **Dividing by Multiples of 10**

- Use long division with two-digit divisors.

Divide, multiply, subtract, bring down.

Use zero as a placeholder.

Place a digit above each digit.

Make sure any remainder is smaller than the divisor.

**Example:** 
$$\begin{array}{r} 19 \text{ R}27 \\ 30 \overline{)597} \\ \underline{30} \\ 297 \\ \underline{270} \\ 27 \end{array}$$

Divide Multiply Subtract Bring down
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- To help divide by a two-digit number, mentally remove the last digit from each number.

**Practice:**

Divide. Remember to write the dollar sign in money problems.

1.  $40 \overline{) \$5.60}$

2.  $20 \overline{) 283} \text{ R}$

3.  $30 \overline{) 630}$

4.  $50 \overline{) \$7.50}$

5.  $10 \overline{) 319} \text{ R}$

6.  $60 \overline{) 254} \text{ R}$

7. Show how to check this division answer. Is the answer correct?

$$\begin{array}{r} 28 \text{ R}24 \\ 30 \overline{) 864} \end{array}$$

Check:  $28 \times \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$

$\underline{\hspace{2cm}} + \underline{\hspace{2cm}} = \underline{\hspace{2cm}}$

Is the quotient correct?  $\underline{\hspace{2cm}}$

**• Multiplying by Three-Digit Numbers**

- When multiplying by three-digit numbers:

Indent using zeros as placeholders.

Carry using mental math if five or less.

Be sure to use commas in the answers.

**Practice:**

Find each product. Carry on your fingers.

1.

$$\begin{array}{r} 412 \\ \times 368 \\ \hline \\ \\ \\ + \phantom{00} \\ \hline \end{array}$$

2.

$$\begin{array}{r} 308 \\ \times 367 \\ \hline \\ \\ \\ + \phantom{00} \\ \hline \end{array}$$

3.

$$\begin{array}{r} 564 \\ \times 293 \\ \hline \\ \\ \\ + \phantom{00} \\ \hline \end{array}$$

4.

$$\begin{array}{r} 405 \\ \times 366 \\ \hline \\ \\ \\ + \phantom{00} \\ \hline \end{array}$$

5.

$$\begin{array}{r} 628 \\ \times 435 \\ \hline \\ \\ \\ + \phantom{00} \\ \hline \end{array}$$

6.

$$\begin{array}{r} 750 \\ \times 547 \\ \hline \\ \\ \\ + \phantom{00} \\ \hline \end{array}$$

• **Multiplying by Three-Digit Numbers That Include Zero**

- Indent using zeros as placeholders.
- “Offset” when the number ends in zero.

$$\begin{array}{r}
 \phantom{0}^1 \\
 324 \\
 \times 140 \\
 \hline
 12960 \\
 + 32400 \\
 \hline
 45360
 \end{array}$$

- When the middle digit in the bottom number is zero, “bring down” the zero.

$$\begin{array}{r}
 \phantom{0}^1 \\
 324 \\
 \times 104 \\
 \hline
 1296 \\
 + 32400 \\
 \hline
 32696
 \end{array}$$

**Practice:**

Multiply. Remember to write the dollar sign in money problems.

1.

$$\begin{array}{r}
 347 \\
 \times 310 \\
 \hline
 \phantom{0} \\
 + \phantom{00} \\
 \hline
 \phantom{00}
 \end{array}$$

2.

$$\begin{array}{r}
 \$2.65 \\
 \times 690 \\
 \hline
 \phantom{0} \\
 + \phantom{00} \\
 \hline
 \phantom{00}
 \end{array}$$

3.

$$\begin{array}{r}
 250 \\
 \times 160 \\
 \hline
 \phantom{0} \\
 + \phantom{00} \\
 \hline
 \phantom{00}
 \end{array}$$

4.

$$\begin{array}{r}
 413 \\
 \times 102 \\
 \hline
 \phantom{0} \\
 + \phantom{00} \\
 \hline
 \phantom{00}
 \end{array}$$

5.

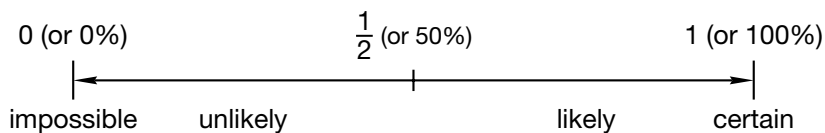
$$\begin{array}{r}
 \$1.86 \\
 \times 201 \\
 \hline
 \phantom{0} \\
 + \phantom{00} \\
 \hline
 \phantom{00}
 \end{array}$$

6.

$$\begin{array}{r}
 260 \\
 \times 208 \\
 \hline
 \phantom{0} \\
 + \phantom{00} \\
 \hline
 \phantom{00}
 \end{array}$$

**• Probability**

- **Probability** measures how likely it is for an event to happen. It is named with a number from 0 to 1.
- **Chance** measures the same thing but with a percent.
- If an event is certain to happen, its probability is 1. Its chance is 100%.
- If an event is impossible, its probability is 0. Its chance is 0%.
- All other events have probabilities between 0 and 1 or chances between 0% and 100%.



- Possible results of experiments that involve probability are called **outcomes**.

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**Practice:**

1. What is the probability a tossed coin will land heads up? \_\_\_\_\_
2. What is the probability a number cube will stop on 3? \_\_\_\_\_
3. What is the probability a number cube will stop on a number less than 6?  
\_\_\_\_\_
4. What is the probability a number cube will stop on a number greater than 6?  
\_\_\_\_\_
5. If a game has a 32% chance of winning, is it more likely that you will win or not win?  
\_\_\_\_\_
6. If there is an 80% chance of rain, then what is the chance that it will not rain?  
Remember to write the percent symbol.  
\_\_\_\_\_

- **Writing Quotients with Mixed Numbers**

- In division problems, sometimes we write the remainder as a fraction.

$$\begin{array}{r} 5 \text{ R}2 \\ 3 \overline{)17} \end{array} \rightarrow \begin{array}{r} 5 \\ 3 \overline{)17} \end{array}$$

**Practice:**

Write each quotient as a mixed number. Show the remainder as a fraction.

1.  $5 \overline{)13}$

2.  $29 \div 4$   $\overline{) \quad}$

3.  $\frac{17}{4}$   $\overline{) \quad}$

4.  $5 \overline{)47}$

5.  $24 \div 5$   $\overline{) \quad}$

4.  $\frac{49}{8}$   $\overline{) \quad}$

7.  $7 \overline{)68}$

8.  $49 \div 10$   $\overline{) \quad}$

9.  $\frac{32}{5}$   $\overline{) \quad}$

10.  $6 \overline{)47}$

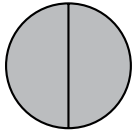
11.  $53 \div 4$   $\overline{) \quad}$

12.  $\frac{51}{8}$   $\overline{) \quad}$

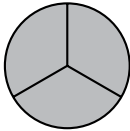


• **Subtracting a Fraction from 1**

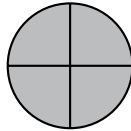
- If the numerator (top) and denominator (bottom) are the same, the fraction equals 1.



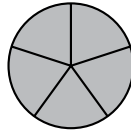
$$\frac{2}{2} = 1$$



$$\frac{3}{3} = 1$$



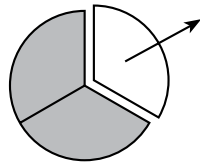
$$\frac{4}{4} = 1$$



$$\frac{5}{5} = 1$$

- When adding fractions and mixed numbers, remember to simplify any fraction names for 1 in the answer.
- To subtract a fraction from 1, rename the 1 as a fraction.

$$\begin{array}{r} 1 - \frac{1}{3} \\ \downarrow \quad \downarrow \\ \frac{3}{3} - \frac{1}{3} = \frac{2}{3} \end{array}$$



- Look at the fraction that is being subtracted to decide which name for 1 to use.

**Practice:**

1. Write a fraction equal to 1 that has a denominator of 5. \_\_\_\_\_

Compare.

2.  $\frac{3}{3} \bigcirc 1$

3.  $3\frac{3}{3} \bigcirc 4$

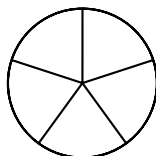
Add.

4.  $\frac{4}{10} + \frac{6}{10} =$  \_\_\_\_\_

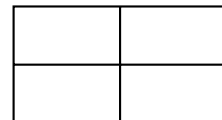
5.  $\frac{3}{8} + \frac{5}{8} =$  \_\_\_\_\_

Subtract. (Rename the 1.)

6.  $1 - \frac{1}{5} =$  \_\_\_\_\_



7.  $1 - \frac{3}{4} =$  \_\_\_\_\_



8. How many fraction names for 1 are there? \_\_\_\_\_

**A** none

**B** 15

**C** 340

**D** infinite

• **Finding a Fraction to Complete a Whole**

- To find a fraction to complete a whole, first rename the 1 with a matching numerator and denominator before subtracting.

**Example:** Two fifths of the students are girls.

What fraction of the students are boys?



**Solution:** This picture shows that the students are  $\frac{5}{5}$ .

The girls are  $\frac{2}{5}$  of the students.

$\frac{5}{5} - \frac{2}{5} = \frac{3}{5}$ , so the boys must be  $\frac{3}{5}$  of the students.

**Practice:**

1. Maggie completed three sevenths of her homework assignment. What fraction of her assignment is left to complete?  
\_\_\_\_\_
2. Four tenths of the skateboarders were able to use a half-pipe without falling. What fraction of the skateboarders were unable to use a half-pipe?  
\_\_\_\_\_
3. Two eighths of the championship football game tickets sold for under \$30. One eighth of the tickets sold for more than \$100. What fraction of the tickets sold for an amount between \$30 and \$100?  
\_\_\_\_\_
4. Yancey ran a mile faster than seven ninths of his classmates. If Yancey ran a mile in 7 minutes 30 seconds, what fraction of his classmates ran the mile in 7 minutes 30 seconds or less?  
\_\_\_\_\_
5. Marlena is learning how to take photographs. She has taken eleven twelfths of the pictures on the roll of film. What fraction of the pictures on the roll of film does she have left to take?  
\_\_\_\_\_