

• Simplifying Improper Fractions

- To simplify improper fractions and mixed numbers:
 1. Divide the numerator of the improper fraction by its denominator. You should get a mixed number result.
 2. Add it to the whole number in the original mixed number.
 3. Reduce as necessary.

Example: $3\frac{12}{5}$

$$\frac{12}{5} = 2\frac{2}{5}$$

$$3 + 2\frac{2}{5} = 5\frac{2}{5}$$

Practice:

Simplify each improper fraction.

1. $\frac{7}{4}$ $4\overline{)7}$

2. $\frac{11}{3}$ $3\overline{)11}$

3. $1\frac{9}{2}$ $2\overline{)9}$

4. $\frac{14}{6}$ $6\overline{)14}$

5. $2\frac{15}{6}$ $6\overline{)15}$

6. $3\frac{13}{3}$ $3\overline{)13}$

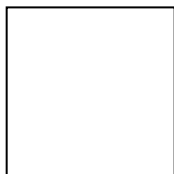
Simplify your answers.

7. $1\frac{2}{3} + 1\frac{2}{3} =$ _____

8. $2\frac{4}{5} + 4\frac{4}{5} =$ _____

9. $\frac{4}{3} \times \frac{3}{2} =$ _____

10. Each side of this square is $\frac{7}{8}$ inches long. What is the perimeter of the square? Remember to write the units.



$\frac{7}{8}$ in.

• **Dividing by Two-Digit Numbers**

- Use long division when dividing by two-digit numbers.
 1. Try the “first digit trick.”
 2. Try compatible numbers.
 3. Then follow the division algorithm.
 4. Use zero as a placeholder in the quotient.

Example:

$$34 \overline{)992}$$

Think: $3 \overline{)9}$

Try 3. If 3 is too much, try 2.

Continue algorithm until finished.

$$\begin{array}{r} \overline{)992} \\ \underline{68} \\ 312 \\ \underline{306} \\ 6 \end{array}$$

Practice:

Divide.

$$1. \overline{)345} \text{ R}$$

$$2. \overline{)964} \text{ R}$$

$$3. \overline{)406} \text{ R}$$

$$4. \overline{)830} \text{ R}$$

$$5. \overline{)361} \text{ R}$$

$$6. \overline{)583} \text{ R}$$

$$7. \overline{)741} \text{ R}$$

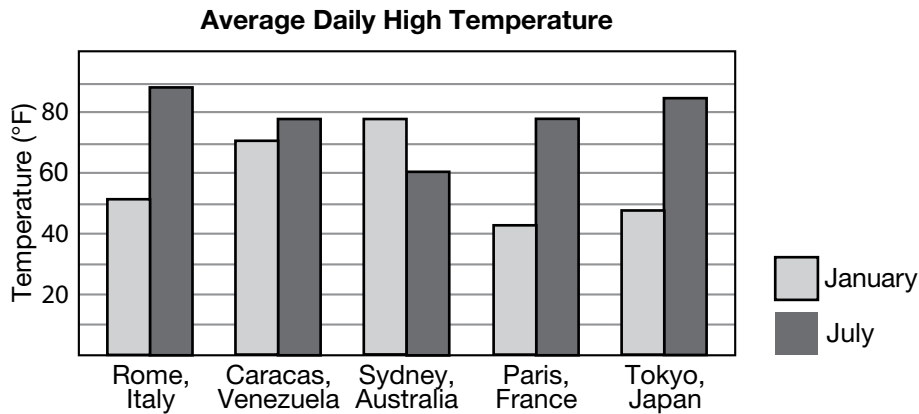
$$8. \overline{)1000} \text{ R}$$

$$9. \overline{)1465} \text{ R}$$

• **Comparative Graphs**

- **Bar graphs** are used to display two or more sets of related data.
- Bar graphs can be horizontal or vertical.

Example: The average daily high temperature in January and July for five cities is displayed in the vertical bar graph below.

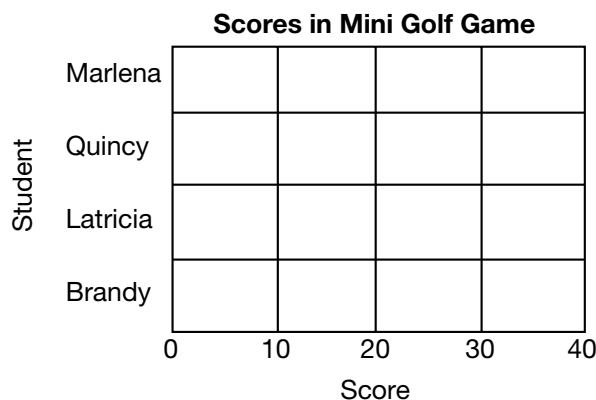


Practice:

1. Marlena, Quincy, Latricia, and Brandy each play two rounds of mini golf. The scores for each student are shown in the table below.

Student	Round 1	Round 2
Marlena	29	23
Quincy	34	28
Latricia	21	29
Brandy	28	30

Make a horizontal bar graph to show the scores. Draw two bars for each player.



• **Using Estimation When Dividing by Two-Digit Numbers**

- Use long division when dividing by two-digit numbers.
 1. Round off the divisor and the dividend before guessing.
 2. Then follow the division algorithm.
 3. Use zero as a placeholder in the quotient.

Example: $18 \overline{)394}$ Think: $20 \overline{)400}$

Try 2.

Continue algorithm
until finished.

$$\begin{array}{r}
 2 1 \text{ R} 16 \\
 18 \overline{)394} \\
 \underline{36} \\
 34 \\
 \underline{18} \\
 16
 \end{array}$$

Practice:

1. $17 \overline{)631} \text{ R}$

2. $32 \overline{)268} \text{ R}$

3. $40 \overline{)820} \text{ R}$

4. $27 \overline{)660} \text{ R}$

5. $27 \overline{)159} \text{ R}$

6. $42 \overline{)719} \text{ R}$

7. $25 \overline{)503} \text{ R}$

8. $37 \overline{)2105} \text{ R}$

9. $28 \overline{)724} \text{ R}$

• Reciprocals

- To write a reciprocal, flip the fraction.

Examples: $\frac{5}{6} \rightarrow \frac{6}{5}$ $\frac{4}{3} \rightarrow \frac{3}{4}$ $4 = \frac{4}{1} \rightarrow \frac{1}{4}$

- The product of any number and its reciprocal always equals 1.

Examples: $\frac{2}{3} \times \frac{3}{2} = \frac{6}{6} = 1$ $\frac{1}{2} \times \frac{2}{1} = \frac{2}{2} = 1$

Practice:

Write the reciprocal of each number. Leave improper fractions as improper fractions.

1. $\frac{3}{7} \rightarrow$ _____

2. $\frac{1}{3} \rightarrow$ _____

3. $\frac{2}{5} \rightarrow$ _____

4. $\frac{4}{9} \rightarrow$ _____

5. $\frac{7}{10} \rightarrow$ _____

6. $4 \rightarrow$ _____

7. $\frac{6}{7} \rightarrow$ _____

8. $\frac{1}{8} \rightarrow$ _____

9. $10 \rightarrow$ _____

10. How many $\frac{5}{12}$ s are in 1? (Use the reciprocal.) _____

11. Divide: $1 \div \frac{3}{5}$ (Use the reciprocal.) _____

12. Think of a fraction and write it down. Then write its reciprocal. Multiply the two fractions. What is the product?

$$\begin{array}{ccccccc}
 \text{---} & & \times & & \text{---} & & = \\
 \uparrow & & & & \uparrow & & \uparrow \\
 \text{fraction} & & & & \text{reciprocal} & & \text{product}
 \end{array}$$

• Using Reciprocals to Divide Fractions

- To use **reciprocals** to divide fractions:

1. Change the \div to a \times .
2. Flip the second fraction to use the reciprocal.
3. Cross cancel (if possible).
4. Multiply across.

Example:

$$\frac{3}{1} \div \frac{3}{4} =$$

↓ ↓

$$\overset{1}{\cancel{3}} \times \frac{4}{\underset{1}{\cancel{3}}} = \frac{4}{1} = 4$$

Practice:

Use the reciprocal to solve.

1. $\frac{1}{5} \div \frac{1}{4} =$

$\frac{1}{5} \times \text{---} = \text{---}$

2. $\frac{2}{7} \div \frac{2}{3} =$

$\frac{2}{7} \times \text{---} = \text{---}$

3. $\frac{2}{5} \div \frac{4}{7} =$

$\frac{2}{5} \times \text{---} = \text{---}$

4. $\frac{3}{2} \div \frac{1}{3} =$

$\frac{3}{2} \times \text{---} = \text{---}$

5. $\frac{4}{8} \div \frac{6}{9} =$

$\frac{4}{8} \times \text{---} = \text{---}$

6. $\frac{10}{3} \div \frac{2}{4} =$

$\frac{10}{3} \times \text{---} = \text{---}$

7. $4 \div \frac{3}{5} =$

$4 \times \text{---} = \text{---}$

8. $7 \div \frac{2}{3} =$

$7 \times \text{---} = \text{---}$

9. $9 \div \frac{1}{4} =$

$9 \times \text{---} = \text{---}$

10. How many $\frac{1}{6}$ s are in $\frac{4}{5}$? $\frac{4}{5} \div \text{---} = \text{---}$

11. How many $\frac{4}{7}$ s are in $\frac{2}{3}$? $\frac{2}{3} \div \text{---} = \text{---}$

• Ratios

- A **ratio** is a way to describe a relationship between numbers. There are three ways to write ratios:

a to b a:b $\frac{a}{b}$

Example: There are four wheels on each car. What is the ratio of wheels to cars?

4 to 1 4:1 $\frac{4}{1}$

- Write the ratio in the order given.
- Reduce a ratio as you would a fraction when possible.
- Leave ratios in fraction form, not as mixed numbers.

Example:

The ratio of red to blue marbles in a bag is 4 to 6.

Write “4 to 6” in fraction form.

We reduce ratios like fractions: $\frac{4 \div 2}{6 \div 2} = \frac{2}{3}$

So the ratio of red to blue marbles is $\frac{2}{3}$. For every two red marbles, there are 3 blue marbles.

Practice:

There are 32 puppies and 48 kittens at the adoption center.

1. What is the ratio of puppies to kittens?

$\frac{\text{puppies}}{\text{kittens}}$ ___ = ___ Reduce.

2. What is the ratio of kittens to puppies?

$\frac{\text{kittens}}{\text{puppies}}$ ___ = ___ Reduce but don't convert.

There were 15 appetizers and 35 entrées at the restaurant.

3. What is the ratio of appetizers to entrées?

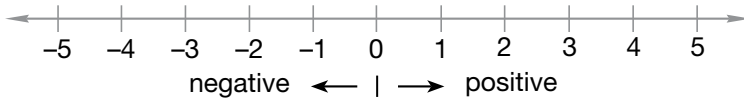
$\frac{\text{appetizers}}{\text{entrées}}$ ___ = ___ Reduce.

4. What is the ratio of entrées to appetizers?

$\frac{\text{entrées}}{\text{appetizers}}$ ___ = ___ Reduce but don't convert.

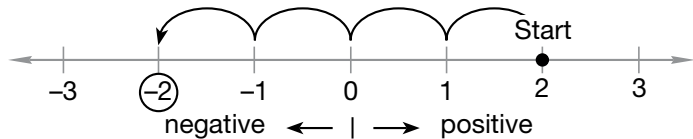
• **Temperature**

- A **thermometer** shows temperature on a scale, which is a kind of number line. **Fahrenheit** and **Celsius** are different temperature scales.
- Units on a temperature scale are called **degrees**.
- We can use a **number line** to understand **negative numbers** and **positive numbers**. Zero is neither negative nor positive.



- Positive numbers are to the right of (greater than) zero.
- Negative numbers are to the left of (less than) zero.
- To subtract using a number line:
 1. Start with the first number given.
 2. Count to the left the number of units to subtract.

Example: $2 - 4 = -2$



Practice:

1. Put a dot at negative five. Label the point with the letter *M*.



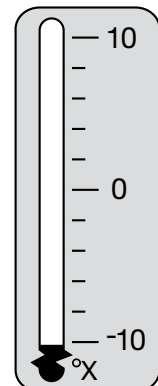
2. Point *R* represents what number on this number line? _____



3. Write the temperature that is 15 degrees below zero on the Fahrenheit scale.

Remember to write the units. _____

4. What temperature is shown on this thermometer? _____
5. Use compatible numbers to estimate the difference in temperature between 23°C and 4°C . _____



• Adding and Subtracting Whole Numbers and Decimal Numbers

- Line up the decimal points.
- Use zeros as placeholders.
- Put a decimal point to the right of any whole number.

Example:

$$\begin{array}{r}
 3.1 + 4.35 + 7 = \quad 3.10 \\
 4.35 \\
 + 7.00 \\
 \hline
 14.45
 \end{array}$$

Practice:

Find each sum or difference.

1.
$$\begin{array}{r} 6.12 \\ + 5 \\ \hline \end{array}$$

2.
$$\begin{array}{r} 8 \\ - 3.67 \\ \hline \end{array}$$

3.
$$\begin{array}{r} 4.03 \\ + 1.94 \\ \hline \end{array}$$

4.
$$\begin{array}{r} 2.59 \\ - 1 \\ \hline \end{array}$$

5. $54 + 8.60 + 22.7 = \underline{\hspace{2cm}}$

6. $15.06 - 12 = \underline{\hspace{2cm}}$

7. $31.4 - 31 = \underline{\hspace{2cm}}$

8. $12 + 1.02 = \underline{\hspace{2cm}}$

9. Compare. $15.00 \bigcirc 15.0$

• Simplifying Decimal Numbers

- Remove extra zeros to the left and right of the decimal point.
- Keep one zero in front of the decimal, if there are no other whole numbers.
- Do not remove zeros between other numerals.

Examples:

$$03.0300 = 3.03$$

$$0.8900 = 0.89$$

Practice:

Simplify each decimal number.

1. $0.420 =$ _____

2. $1.200 =$ _____

3. $05.9010 =$ _____

4. $10.800 =$ _____

5. $08.9320 =$ _____

6. $7.000900 =$ _____

Simplify each answer.

$$\begin{array}{r} 7. \quad 4.38 \\ + 3.62 \\ \hline \end{array}$$

$=$ _____

$$\begin{array}{r} 8. \quad 10.98 \\ - 8.88 \\ \hline \end{array}$$

$=$ _____

$$\begin{array}{r} 9. \quad 5.56 \\ + 3.34 \\ \hline \end{array}$$

$=$ _____

10. Attach a zero to 3.05 without changing its value. _____

11. Attach a zero to 8 without changing its value. _____

12. Explain why attaching a zero at the end of a decimal number is unlike attaching a zero to the end of a whole number. See the example below.

$3.0 \rightarrow$ attach a zero $\rightarrow 3.00$ $3 \rightarrow$ attach a zero $\rightarrow 30$
